Technical Note: Time lag correction of aquatic eddy covariance data measured in the presence of waves

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Abstract

Extracting benthic oxygen fluxes from eddy covariance time series measured in the presence of surface gravity waves requires careful consideration of the temporal alignment of the vertical velocity and the oxygen concentration. Using a model based on linear wave theory and measured eddy covariance data, we show that substantial erroneous fluxes can arise if these two variables are not aligned correctly in time. We refer to this error in flux as the time lag bias. In one example, produced with the wave model, we found that an offset of 0.25 s between the oxygen and the velocity data produced a two-fold overestimation of the flux. In another example, relying on nighttime data measured over a seagrass meadow, a similar offset reversed the flux from an uptake of $-50 \text{ mmol m}^{-2} \text{ d}^{-1}$ to a release of $40 \text{ mmol m}^{-2} \text{ d}^{-1}$. The bias is most acute for data measured at shallow-water sites with short-period waves and low current velocities. At moderate or higher current velocities ($>5-10 \text{ cm s}^{-1}$), the bias usually is insignificant. The widely used traditional time shift correction for data measured in unidirectional flows, where the maximum numerical flux is sought, should not be applied in the presence of waves because it tends to maximize the time lag bias. Based on wave model predictions and measured data, we propose a new time lag correction that minimizes the time lag bias. The correction requires that time series of both vertical velocity and oxygen concentration contain a clear periodic wave signal. Because wave motions are often evident in eddy covariance data measured at shallow-water sites, we encourage more work on identifying new time lag corrections. On that premise, we make all raw data used in this study available to interested users.
1 Introduction

1.1 Background

Eddy covariance (or eddy correlation) measurements of scalar fluxes under water have been performed for many years with the earliest studies focusing on measurements of heat fluxes under sea ice (McPhee, 1992; Fukuchi et al., 1997; Shirasawa et al., 1997) and salt fluxes in a salt wedge estuary (Partch and Smith, 1978). More recently, concurrent heat and salt fluxes have also been measured over marine permeable sandy sediments as tracers for groundwater seepage (Crusius et al., 2008). Over the last 10 years, the aquatic eddy covariance technique has become a widely accepted approach for measuring oxygen fluxes between benthic ecosystems and the overlying water (Berg et al., 2003). In that time, it has been applied under very different field settings such as arctic muddy and sandy sediments (Glud et al., 2010), subtropical coral reefs (Long et al., 2013), and temperate seagrass meadows (Rheuban et al., 2014). With a few exceptions, all recent published aquatic eddy covariance studies have focused on oxygen fluxes. Oxygen fluxes are also the focus of this study, but its findings apply to all scalar fluxes.

The aquatic eddy covariance technique has clear advantages over other methods for measuring fluxes between the benthic environment and the overlying water, including its non-invasive nature (Lorrai et al., 2010), high temporal resolution (Rheuban and Berg, 2013), and ability to integrate over a large benthic surface (Berg et al., 2007). As a result, the technique is poised for widespread use in aquatic science, analogous to the development in atmospheric boundary layer research where the equivalent approach is now the preferred standard method for measuring land–air fluxes (Baldocchi, 2003). As part of the development of the technique in aquatic environments, a few challenges must be addressed. Procedures for calculating fluxes from raw data must be refined further to minimize errors and uncertainties. The ones used today are largely adapted directly from atmospheric boundary layer research, where the eddy covariance technique has been used for more than six decades (Priestley and Swinbank, 1971).
1947; Swinbank, 1951). For the aquatic environment, however, only a limited number of papers have had scalar flux calculation methodologies as their main focus (Shaw and Trowbridge, 2001; Reimers et al., 2012; Holtappels et al., 2013).

1.2 Formulation of problem

This study focuses on estimating oxygen fluxes under a set of field conditions that do not occur in the atmosphere, but are very common under water at shallow-water sites. Here, surface gravity waves can cause oscillatory motion throughout the water column to the benthic surface, and give rise to a unique set of challenges when eddy fluxes are extracted. Some of these challenges are directly linked to limitations of the eddy covariance instrumentation available today. Although fast-responding oxygen sensors are used in eddy covariance measurements, their speed is still limited relative to the velocity sensor (e.g. a Vector Acoustic Doppler Velocimeter (ADV) from Nortek AS). Clark-type oxygen microelectrodes used for eddy covariance typically have response times ($t_{90\%}$) of 0.2 to 0.4 s (Revsbech, 1989; Berg et al., 2003; Holtappels et al., 2015). Newer optical sensors that have been developed in recent years have somewhat longer response times of 0.3 and 1 s (Chipman et al., 2012; Murniati et al., 2015; Berg et al., 2015). This means that the time series of the two key variables from which eddy fluxes are derived, the vertical velocity and oxygen concentration, are never perfectly aligned in time with the oxygen concentration lagging behind the velocity. Also, because the ADV derives its data from acoustic backscatter of suspended particles moving through its $\sim 2$ cm$^3$ measuring volume, the oxygen sensor must be positioned outside of this volume to avoid disturbing the velocity measurements. Depending on the instantaneous flow direction and magnitude, this can increase or decrease the time lag between the two time series.
1.3 Traditional time lag correction

For measurements in unidirectional flows with thin fast-responding Clark-type micro-electrodes that can be positioned at the edge of the ADV’s measuring volume, the temporal misalignment usually has insignificant effects on the flux estimate (Berg et al., 2013). Inspection of the cumulative co-spectrum between the vertical velocity and the oxygen concentration can confirm or reject this on a case-by-case basis (Lorrai et al., 2010; Berg et al., 2013). In situations when the misalignment does affect the calculated eddy flux, a straightforward correction has been adapted from atmospheric boundary layer research, in which the oxygen data are successively shifted in time relative to the velocity data in order to find the maximum numeric flux, or cross-correlation (Fan et al., 1990; McGinnis et al., 2008; Lorrai et al., 2010). Figure 1 shows an example of this correction based on data measured in a river with a unidirectional flow of \( \sim 16 \text{ cm s}^{-1} \) using a new dual oxygen-temperature sensor with a 1 cm tip diameter (Berg et al., 2015) positioned 1.5 cm downstream from the ADV’s measuring volume (edge to edge).

1.4 Scope of work

We will show that even small temporal misalignment between the vertical velocity and the oxygen concentration, inherently imbedded in all present eddy covariance data, can lead to significant errors in fluxes extracted from data measured in the presence of waves. We refer to this error as the time lag bias, and show that the traditional time lag correction illustrated in Fig. 1 will likely fail. Using a model based on linear wave theory and measured data; we explain the cause of the bias and examine its potential magnitude. We then propose a new correction for this time lag, which minimizes the time lag bias, and test it on two sets of measured data. We encourage more work on identifying new time lag corrections and provide a link from where all of the raw data used in this study can be downloaded.
2 Methods

2.1 Illustration of the problem using a wave model

The two-dimensional model for progressive waves and their effect on the oxygen concentration at a fixed height above the sediment surface is presented in the Appendix. In short, the model describes the horizontal and vertical wave orbital velocities and the variation in oxygen concentration generated by the up-and down movement of the natural oxygen gradient as a function of time as they would be recorded under ideal conditions, without any time lag and at exactly the same location. Parameters for the model were estimated using eddy covariance data reported by Berg and Huettel (2008) from a shallow-water site exposed to surface waves. The model was used to generate theoretical time series of the wave velocity and wave-generated variation in oxygen concentration that were then shifted in time relative to one another to illustrate how a time lag can affect the flux calculation.

Using the parameter values listed in Table A1 (Appendix), the model was found to mimic the averaged nighttime conditions reported by Berg and Huettel (2008) well. As illustrated in Fig. 2a, the simulated vertical wave velocity ($\tilde{w}$) varied between $\sim \pm 2 \text{ cm s}^{-1}$, while the associated up-and down movement of the natural oxygen gradient caused by the sediment’s uptake produced $\text{O}_2$ concentration oscillations ($\tilde{O}_2$) of $\sim \pm 1 \mu\text{mol L}^{-1}$. These modeled data are for the case where the velocity and oxygen concentration are “recorded” without any time lag and at exactly the same location. Furthermore, these data exclude any current-driven turbulence so that variations in velocity and concentration are due to wave orbital motion only. The significant time lag bias, which can arise from the wave signal alone in eddy covariance data, becomes apparent when shifting the oxygen data stepwise in time relative to the velocity data and recalculating the eddy flux for each shift (Fig. 2b).

The model and its results in Fig. 2 reveal key characteristics of the time lag bias due to waves:
1. As soon as there is a time lag between the velocity and the oxygen measurements (time shift ≠ 0, Fig. 2b), a bias in the flux estimate will arise.

2. The size of the time bias scales with the mean oxygen concentration gradient in the water column, therefore, it scales with the real flux.

3. The time lag bias can have the opposite sign of the real flux.

4. The maximum time lag bias can exceed the real flux.

5. For short-period waves, here 2.3 s, a time lag of only 0.20 s can give a bias equal to the real flux.

6. Because oxygen sensors do not have an instant response, and because velocity and oxygen data are not measured at exactly the same location, fluxes may be biased if wave-driven fluctuations in velocity and oxygen concentration can be identified.

7. The traditional time shift correction, which works well in unidirectional flow (Fig. 1), will tend to identify the time shift associated with the maximum time lag bias.

8. The time lag bias can be eliminated if the appropriate time shift is applied (Fig. 2b).

The vertical gradient in oxygen concentration is less pronounced for field situations with substantial vertical turbulent mixing. As a result, eddy fluxes calculated from data measured at sites with significant unidirectional currents and rough sediment surfaces, both stimulating vertical mixing (Rattray and Mitsuda, 1974; Boudreau and Jorgensen, 2001), will be less sensitive to time lag bias, even if orbital wave motions are present. The example in Fig. 2, where the maximum bias was found to be 180 % of the real flux, was based on a mean current velocity of 1.0 cm s\(^{-1}\) and a sediment surface roughness parameter of 2 mm (Table A1). For rougher surfaces, for example one with a roughness 10 mm, additional simulations showed that the maximum bias decreased from 180 to
110\% of the real flux. A much larger reduction in maximum bias was seen with increasing current velocity as illustrated in Fig. 3. For example, an increase in velocity from 1 to 5 cm s\(^{-1}\) or from 1 to 10 cm s\(^{-1}\) reduced the time lag bias by a factor of 5 and 10, respectively.

When using the eddy covariance instrumentation available today, there will always be a time lag between the velocity and the oxygen data; therefore, the sensitivity of the flux calculation to even small time lags, as documented in Fig. 2b, can compromise the eddy flux estimated from data measured in the presence of waves.

### 2.2 Illustration of new time lag correction using wave model data

In addition to illustrating the time lag bias, the modeled data in Fig. 2a also point to a new correction. From \(\tilde{w}\), the vertical displacement due to wave orbital motion, \(\tilde{z}\), can be estimated as

\[
\tilde{z} = \int \tilde{w} dt
\]

This variable, also shown in Fig. 2a, expresses the instantaneous relative elevation of a water parcel that is moved up and down at the vertical wave orbital velocity \(\tilde{w}\). Defining the positive \(z\) direction upward, \(\tilde{z}\) increases when \(\tilde{w}\) is positive, and vice versa (Fig. 2a). Due to the positive gradient in mean oxygen concentration created by the sediment’s consumption of oxygen, a minimum in \(\tilde{O}_2\) will coincide exactly with a maximum in \(\tilde{z}\) in the absence of a time lag, and vice versa (Fig. 2a). Because this combination corresponds to a minimum in cross-correlation of \(\tilde{z}\) and \(\tilde{O}_2\), a new correction for the time lag in measured data can be defined by shifting the \(\tilde{O}_2\) data relative to the \(\tilde{z}\) data until this minimum is located. If instead, the sediment releases oxygen due to benthic photosynthetic production, the mean oxygen concentration gradient is negative and a minimum in \(\tilde{O}_2\) will be matched by a minimum in \(\tilde{z}\), and vice versa. In this case, the time lag correction can be defined as giving a maximum in cross-correlation of \(\tilde{z}\) and \(\tilde{O}_2\). As a result of these two different situations, in which the sediment consumes
or releases oxygen, a general correction can be defined by locating maxima or minima in the cross-correlation of $\tilde{z}$ and $\tilde{O}_2$. Complications in this correction arise if there is no clear vertical gradient in mean oxygen concentration, for example at dawn and dusk, when oxygen production may match respiration, or in situations where vertical mixing due to substantial current is so vigorous that the vertical oxygen gradient diminishes. These cases are discussed in detail below.

### 2.3 Illustration of new time lag correction using measured data

Figure 4 shows an example of the new correction applied to a 15 min measured eddy covariance data segment, which is the typical time interval used to calculate one eddy flux value (Berg et al., 2003). The data were measured over a dense seagrass meadow using a new robust oxygen optode with no stirring sensitivity and a response time ($t_{90\%}$) of 0.51 s when inserted from air into a water bath (Berg et al., 2015). The measuring height was 30 cm above the sediment surface, water depth was 90 cm, significant wave height 5 cm, and the mean current velocity 0.8 cm s$^{-1}$. To isolate the wave signal from other less dynamic variations in the velocity and oxygen concentration before calculating the cross-correlation of $\tilde{z}$ and $\tilde{O}_2$, and also to minimize noise, a 231 data point (3.61 s) running average was removed from the raw 64 Hz data and the result was smoothed by a 17 point (0.27 s) running average. An example of the resulting data is shown in Fig. 4a. The eddy flux itself was calculated from the raw unprocessed data following standard flux calculation procedures based on linear de-trending (Lee et al., 2004; Berg et al., 2009; Attard et al., 2014). Therefore, the estimated eddy flux represents the real flux plus any time lag bias.

The 15 s data segment in Fig. 4a shows a distinct wave signal in $\tilde{z}$ and $\tilde{O}_2$, which is a prerequisite for the time lag correction to work. Furthermore, these results, based on measured data, confirm the modeled results shown in Fig. 2, and reveal that the eddy flux (here the real flux plus the time lag bias) can vary substantially and attain both positive and negative values depending on the time shift applied (Fig. 4b). The results underline the notion that obtaining the best estimate of the real flux hinges on a properly
determined time shift. In this case, the corrected flux was associated with a time shift of 0.78 s, defined by a distinct minimum in cross-correlation of $\tilde{z}$ and $\tilde{O}_2$ (Fig. 4b). This shift should be seen in relation to the sensor’s own response time ($t_{90\%} = 0.51$ s). These values and how they relate are discussed in detail below. The correction reduced the derived flux from $-123$ to $-51$ mmol m$^{-2}$ d$^{-1}$, or to a value corresponding to 42\% of the non-corrected flux (Fig. 4c). Finally, the data revealed that the traditional time shift correction, where the maximum numerical flux is sought, will lead to substantial overestimation of the flux (Fig. 4c).

3 Results

The new time lag correction was tested on two eddy covariance data sets that were 4 and 16 h long. Both were measured at shallow-water sites and were characterized by relatively low current velocities and short-period waves, which caused clear wave-driven fluctuations in vertical velocity and oxygen concentration. Consequently, these two data examples had the characteristics expected to produce sizeable time lag biases.

3.1 Application of new time lag correction, first example

The first data set (Fig. 5) was measured at dusk over the same dense seagrass meadow and with the same fast-responding oxygen optode (Berg et al., 2015) as described in Sect. 2.3. The measuring height again was 30 cm above the sediment.

The 60 s data segment (Fig. 5a) shows, as the previous example (Fig. 4a), a distinct wave signal in $\tilde{z}$ and $\tilde{O}_2$ with a $\sim 1.5$ s period. Wave groups (i.e. sets of 1.5 s waves) with a $\sim 11$ s period are also visible. The significant wave height averaged 4 cm (Fig. 5b), and the current changed in direction and also in strength between 0.2 and 2.5 cm s$^{-1}$ with an average of 1.0 cm s$^{-1}$, while the water depth varied between 80 and 140 cm. Unambiguous variations in $\tilde{z}$ and $\tilde{O}_2$, with amplitudes of $\sim 0.5$ cm and $\sim 0.5$ µmol L$^{-1}$,
respectively, allowed precise determination of minima in cross-correlation of $\tilde{Z}$ and $\tilde{O}_2$ which gave virtually the same time shift for every 15 min time interval used for individual flux estimates (Fig. 5c). The averaged time shift was $0.84 \pm 0.013$ s (SE, $n = 16$), and the correction reduced the averaged flux from $-117 \pm 8.9$ to $-68 \pm 9.7$ mmol m$^{-2}$ d$^{-1}$ (SE, $n = 16$), or by a factor of 0.58 (Fig. 5d).

3.2 Application of new time lag correction, second example

The 16 h long data set, covering a period from late afternoon into the next day, was measured over a permeable sandy sediment as previously reported by Berg and Huettel (2008). The measuring height was 12 cm above the sediment, and the oxygen concentration was measured with a Clark-type microelectrode. Parameters for the wave model (Figs. 2 and 3) were determined from nighttime data from this deployment.

The 60 s data segment shown in Fig. 6a depicts the time when the wave action was at its maximum (Time $\sim 620$ min). Currents were stronger and waves larger during this deployment, but the segment contains the same clear correlations between the wave driven fluctuation in $\tilde{Z}$ and $\tilde{O}_2$ as found in the previous examples (Figs. 4a and 5a). The period of the waves was $\sim 2.3$ s and the variation in $\tilde{Z}$ and $\tilde{O}_2$ had amplitudes of $\sim 1$ cm and 2.5 µmol L$^{-1}$, respectively. The significant wave height averaged 13 cm (Fig. 6b), and the current velocity changed in direction and also in strength between 0.6 and 5 cm s$^{-1}$ (Fig. 6b) with an average of 2 cm s$^{-1}$. In only 2 of the 67 time intervals used for individual flux estimates, each 15 min long, no extremum was found in the cross-correlation of $\tilde{Z}$ and $\tilde{O}_2$. The optimum time shift corresponded to a minimum correlation for the first part of the deployment (Time $< 1200$ min) when the oxygen flux was negative, and a maximum correlation for the rest of the deployment, consistent with an oxygen release (Fig. 6c). Averaged over the night, the correction reduced the flux from the previously reported $-368 \pm 21$ mmol m$^{-2}$ d$^{-1}$ (SE, $n = 45$) to $-220 \pm 21$ (SE, $n = 43$) mmol m$^{-2}$ d$^{-1}$, or by a factor of 0.60 (Fig. 6d). This corrected flux is still roughly twice the size of the flux derived from concurrent in situ chamber measurements (Huettel and
Gust, 1992; Berg and Huettel, 2008). The averaged time shift for the entire deployment was $1.18 \pm 0.04$ s (SE, $n = 65$).

4 Discussion

The results of this study show that oxygen fluxes extracted from eddy covariance data measured at shallow-water sites with short-period waves and low current flows can be affected by a so-called “time lag bias”. The bias arises because of displacement of the natural vertical oxygen gradient by wave orbital motions, combined with temporal misalignments of the oxygen concentration time series relative to the vertical velocity data. This misalignment cannot be entirely avoided with any eddy covariance instrumentation for aquatic scalar flux measurements available today. As a result, time lag bias, documented here using both modeled and measured data, should be considered when eddy covariance data are measured under such field conditions. Time lag corrections that will minimize this bias are possible, and one is presented in this study.

The theoretical example (Fig. 2), produced with a simple model based on linear wave theory (Appendix) and fitted to measured data reported by Berg and Huettel (2008), illustrates that the time lag bias can be substantial. The modeled data (Fig. 2a), where all variations were due to wave orbital motions, contain no time lag and represent an idealized situation in which velocity and oxygen data were aligned perfectly in time and space. In this case, there is no time lag bias (time shift $= 0$, Fig. 2b). The data also showed that an imposed time shift of the oxygen data relative to the velocity data of only 0.20 s led to a bias of 100 % of the real flux (Fig. 2b), and that the maximum bias, equaling 180 %, was found at a time shift of 0.58 s. The model parameters that gave these substantial time lag biases, including an 11 cm surface displacement amplitude of the waves and a current velocity of 1 cm s$^{-1}$ (Appendix), represent common conditions at many near-shore sites. Additional model calculations showed that the maximum bias diminishes rapidly at increasing current velocity due to enhanced turbulent mixing,
which reduces the vertical oxygen concentration gradient (Fig. 3, Appendix). Thus, time lag bias should usually only be of concern under relatively low-current flow conditions.

The modeled example also shows that if the oxygen concentration and the vertical velocity are aligned correctly in time, there is no time lag bias (Fig. 2b), thus points to the foundation of the correction proposed in this study. This correction identifies the time shift that gives a minimum in cross-correlation of the wave-generated fluctuation in oxygen concentration ($\tilde{O}_2$) and the vertical displacement ($\tilde{z}$, Eq. 1) in situations when the benthic system takes up oxygen (Fig. 4b). Opposite to this, where the system releases oxygen, a maximum in cross-correlation is sought.

Essentially, the same correction could be defined by using the cross-correlation between $\tilde{O}_2$ and either the fluctuating water pressure or horizontal wave velocity. The pressure is recorded by standard ADVs at the same sampling frequency as the velocity and usually at very low noise levels. However, the ADV we are using (a fixed stem Vector from Nortek AS) measures the pressure at its lower end bell which is located $\sim 37$ cm above the ADV’s measuring volume where the velocities are measured. As a result, even a small tilt of the ADV during measurements can introduce a time lag between the cross-correlated variables and lead to false corrections. Similarly, the horizontal wave velocity is split in two when recorded as the ADV’s two horizontal $x$ and $y$ velocities. Thus, a rather complex rotation is needed to obtain the horizontal wave velocity (Reimers et al., 2012). In addition, the ADV’s $x$ and $y$ velocities are associated with substantially higher noise levels than the vertical $z$ velocity. For these reasons, we chose the integrated vertical wave velocity (Eq. 1) for the new time lag correction.

An attractive feature of the correction is its simplicity, but it has limitations too as it requires that both the measured vertical velocity and the oxygen concentration contain a clear periodic wave signal. Consequently, at shallow-water sites with photosynthesizing sediment surfaces, it may fail during shorter periods at dusk and dawn when the oxygen flux changes from a release to an uptake, or vice versa, reversing the vertical mean oxygen concentration gradient. Likewise, the correction may also fail, if the wave signal cannot be clearly identified due to broad-spectrum wave activity.
The new correction identifies one single time shift that is applied to the entire time interval, typically 15 min, for which a flux is calculated (Figs. 4c, 5c and 6c). Although most of the temporal misalignment of the oxygen data relative to the velocity data is caused by the oxygen sensor’s response time, the physical distance between the ADV’s measuring volume and the oxygen sensors can play a role too. Because the horizontal wave velocity fluctuates and reverses in direction in each wave cycle, the optimal instantaneous time shift varies somewhat in time. It is unknown how much the use of one single time shift for each individual flux calculation affects the correction.

A future refinement of a time lag correction would be to include two contributions, a larger constant one representing the response time of the oxygen sensor, and a smaller dynamic one accounting for the spatial separation between the velocity and the oxygen sensor. The latter contribution, which would obtain both positive and negative values, could easily be determined from known instantaneous horizontal $x$ and $y$ velocities relative to the position of the two sensors. As an added benefit, this proposed correction would be more versatile and work in both unidirectional and wave-driven flows.

Another possible correction would be to remove the flux contribution associated with waves in the frequency domain, as opposed to the time domain used here. This flux contribution can be identified fairly easily in the co-spectrum or cumulative co-spectrum of the vertical velocity and the oxygen concentration, and then removed. This, or similar approaches, are already widely used to remove wave contributions to Reynolds stresses for wave dominated near-bottom flows (Bricker and Monismith, 2007). However, such corrections should be applied with caution here because part of the real vertical oxygen flux may be facilitated by wave motions, and thus occur at the wave frequency. Wave motions over rough benthic surfaces can give rise to eddies or water parcel ejections at wave frequencies, which expand up into the bottom water, well above the wave boundary layer (Kemp and Simons, 1982; Sleath, 1987; Reidenbach et al., 2007).
The removal of wave contributions to the covariance of vertical and horizontal velocity components, usually termed wave bias in Reynolds stress calculations, addresses a somewhat similar, yet different problem than that focused on here. Wave bias arises from an angular misalignment of the ADV relative to the principal axes of the wave-induced velocity field and is usually caused by sensor tilt (Grant and Madsen, 1986; Trowbridge, 1998; Shaw and Trowbridge, 2001). Although there is no time lag between the horizontal and the vertical velocity components, which are measured by the same instrument, this angular misalignment can cause significant artificial contributions to Reynolds stress estimates. The time lag bias addressed here is caused by a temporal misalignment between the velocity and the oxygen concentration measured with two individual sensors.

The relatively large time lag bias found in the modeled example (Fig. 2) was also seen in the measured data example recorded over a dense shallow-water seagrass meadow (Fig. 4). The data, covering a 15 min time interval, had an inherent time lag between the measured oxygen concentration and the velocity, and showed a similar high sensitivity to imposed time shifts (Figs. 4b vs. 2b). For example, time shifts of 0, 0.27, and 0.47 s led to eddy fluxes, here representing the real flux plus time lag bias, of −117, 0, and 40 mmol m\(^{-2}\) d\(^{-1}\), respectively, or a change from a clear uptake, to no flux, to a clear release (Fig. 4b). This rather extreme, but real, example also shows how important it is to identify the appropriate time shift to minimize the time lag bias. It further illustrates how the traditional time shift correction, where the maximum numerical flux is sought, would tend to give the maximum time lag bias (Fig. 4b).

The wave-driven periodic variation in \(\tilde{O}_2\) and \(\tilde{z}\) (Fig. 4a) produced a clear minimum in cross-correlation of these two variables that could easily be located (Fig. 4b). This minimum occurred at a time shift of 0.78 s, which gave a corrected flux that was 42% of the uncorrected flux (Fig. 4c). For reference, the optimal time shift found for the same oxygen sensor in unidirectional river flow was on average 0.83 s (Berg et al., 2015) and 0.88 s in the example shown here in Fig. 1. The sensor's own response time (\(t_{90\%}\)) was measured in lab tests to be 0.51 s, when inserted from air into water baths. The
somewhat slower response found in the field, where the sensor was permanently under water, was likely caused by oxygen concentration equilibration through the thin boundary layer flow that forms on the oxygen sensing foil (Berg et al., 2015). Through detailed model calculations, Berg et al. (2015) showed that a sensor with this response time will virtually capture the entire flux signal if a time lag correction is applied. Specifically, the underestimation of the flux was found to be less than 5%, even in challenging situations at shallow-water sites with substantial unidirectional current flow, where small rapid eddies dominated the vertical turbulent mixing.

In both of the two longer-period data examples covering 4 and 16 h (Figs. 5 and 6), the new time lag correction led to considerable reductions in the derived eddy flux. In the first example, including 16 individual flux estimates, each based on 15 min time intervals (Fig. 5c), the average corrected flux was 58% of the uncorrected flux (Fig. 5d), and the time shifts were very similar across all time intervals (Fig. 5c). The fact that fluctuating variations in velocity and oxygen concentration included both longer-period wave groups and short-period waves (Fig. 5a) did not prevent location of optimal time shifts. In the second example, which used data reported earlier by Berg and Huettel (2008) and including 67 individual flux estimates (Fig. 6c), the average corrected nighttime flux was 60% of the uncorrected flux (Fig. 6d). The individual time shifts showed more variation than in the previous example (Fig. 6c). The relatively large variation was likely caused by the more pronounced variations in the two horizontal velocities and significant wave height (Fig. 6b). The relatively large average time shift was not expected because Clark-type electrodes used for eddy covariance typically have response times (t_{90%}) between 0.2 to 0.4 s (Revsbech, 1989; Berg et al., 2003; Holtappels et al., 2015). The most likely reason for the large shift is that the electrode was damaged or coated with phyto-detritus near the beginning of the deployment, for example at min ∼ 460 (Fig. 6c), when the time shift abruptly doubled from a value well below 1 s. However, it should be noted that the large time shift is not the reason for the substantial reduction in oxygen flux associated with the correction. In examples given above, much smaller time shifts had similar large effects on the flux (Figs. 2b and 4b). The corrected flux
is still roughly twice the size of the flux that was measured with in situ chambers deployed concurrently (Fig. 6d). Fundamental differences between the two flux methods, especially when applied to permeable sandy sediments, may explain this disagreement (Glud, 2008; Reimers et al., 2012; Berg et al., 2013).

The data in Figs. 4 and 5 were measured with a new robust oxygen optode that in lab tests showed no stirring sensitivity (Berg et al., 2015), whereas the data in Fig. 6 were recorded with a Clark-type microelectrode, a sensor-type that is known to be affected by the instantaneous water velocity at its tip due to its consumption of oxygen (Gust et al., 1987; Revsbech, 1989; Gundersen et al., 1998). Two new studies have focused on how this stirring sensitivity can affect eddy flux estimates in unidirectional flows (Holtappels et al., 2015) and in wave environments (Reimers et al., 2015). We cannot rule out that the oxygen measurements shown in Fig. 6 were affected to some extent by the varying wave velocity. However, typical characteristic patterns of stirring sensitivity in wave environments as documented by Reimers et al. (2015) were not seen in these data. Firstly, stirring sensitivity tends to have an asymmetric dependency on wave velocity, meaning that oxygen concentration is more affected by the velocity from one direction than from the other (Holtappels et al., 2015; Reimers et al., 2015). Signs of this characteristic pattern are easy to identify, but were not seen in our data (Fig. 6a), which contained more of a sinusoidal variation in oxygen concentration. Secondly, if instead stirring sensitivity presents itself as a symmetric dependency of wave velocity, which can happen for example if the fluctuating velocity is perpendicular to the sensor, it would appear as a fluctuation in concentration with a frequency double that of the wave frequency. This also was not seen in our data (Fig. 6a). Thirdly, stirring sensitivity for a specific microelectrode will likely appear as a close-to-constant reduction or increase of the flux. The fact that we found a close, and highly realistic, correlation of oxygen flux to light (Fig. 6c), both in the original data (Berg and Huettel, 2008) and in the corrected data (Fig. 6c), suggests that stirring sensitivity was not a dominant part of the microelectrode signal. We, therefore, assess that stirring sensitivity did not play a significant role in any of the data presented in this study.
5 Summary and recommendations

The results presented here illustrate that substantial time lag biases can arise in flux estimates from eddy covariance data measured in the presence of surface gravity waves. The problem is most acute for data measured at shallow-water sites with short-period waves and low current flows. At moderate or high current velocities (> 5 to 10 cm s\(^{-1}\)), the bias usually is insignificant under typical field conditions. The problem can be effectively addressed by applying the appropriate correction.

A simple, but helpful, additional flux calculation that will indicate if time lag bias should be of concern, is to impose a small time shift (∼ 0.1–0.2 s) on the measured raw data and re-calculate the flux. If a significant change in flux is found, time lag bias should be further investigated.

The widely used traditional time shift correction in unidirectional flows, where the maximum numerical flux is sought, tends to amplify the time lag bias and should not be applied if clear wave signals are seen in the data. Although the new correction presented here will minimize the time lag bias, one should always strive to measure eddy covariance data using oxygen sensors with minimum time delay and to measure both the velocity and the oxygen concentration as close to the same location as possible.

We encourage more work on these issues because wave motion more often than not appears in eddy covariance data measured at shallow-water marine sites.

5.1 Access to data used in this study

To facilitate more work on eddy flux calculation from data measured in the presence of waves, the data used in this study can be downloaded from: http://faculty.virginia.edu/berg/.
Appendix

A model for wave orbital velocities associated with progressive linear waves and their effect on the oxygen concentration at a given height over the sediment surface was developed and fitted to existing measured eddy covariance data. The model was used to generate theoretical time series of the wave orbital velocity and the corresponding oxygen concentration at the measuring point of an eddy covariance system. These time series were then shifted in time relative to one another to illustrate how a time lag can bias the flux calculation.

The horizontal and vertical wave orbital velocity components, \( \tilde{u} \) and \( \tilde{w} \), can be expressed as (Dean and Dalrymple, 1991)

\[
\tilde{u} = a\omega \frac{\cosh(kh)}{\sinh(kH)} \cos(-\omega t) \quad (A1)
\]

and

\[
\tilde{w} = a\omega \frac{\sinh(kh) \sinh(kH)}{\sinh(kH)} \sin(-\omega t) \quad (A2)
\]

where \( a \) is the wave surface displacement amplitude, \( \omega \) the angular frequency \((\omega = 2\pi f, f \) is the wave frequency in Hz), \( k \) is the angular wavenumber \( (k = 2\pi/\lambda, \lambda \) is the wave length), \( h \) is the measuring height above the bottom, and \( H \) is the total water depth.

A value of \( k \) (or \( \lambda \)) is difficult to assess from measured velocity time series, but can be estimated from the dispersion equation (Dean and Dalrymple, 1991) that relates \( k \), \( \omega \), and \( H \) as \( \omega = \sqrt{gk \tanh(kH)} \) where \( g \) is the acceleration due to gravity. Rearranging this equation, \( k \) can be calculated by iteration as

\[
k_{i+1} = \frac{\omega^2}{g \tanh(k_i H)} \quad (A3)
\]
where \( i \) is the iteration step number.

The relative vertical displacement of a water parcel, \( \tilde{z} \), can be found by integrating Eq. (A2).

\[
\tilde{z} = \int_{0}^{t} \tilde{\omega} dt = a \frac{\sinh(kh)}{\sinh(kH)} \cos(-\omega t)
\]  

(A4)

Assuming that a vertical gradient in mean oxygen concentration, \( \frac{d\tilde{C}}{dz} \), exists near the bottom due to the uptake or release of oxygen by the sediment, the relative concentration fluctuation can be approximated to first order as

\[
\tilde{C} \sim \frac{d\tilde{C}}{dz}(\tilde{z}) = -a \frac{d\tilde{C}}{dz} \frac{\sinh(kh)}{\sinh(kH)} \cos(-\omega t)
\]  

(A5)

The vertical gradient can be estimated from Fick’s first law of diffusion applied to vertical turbulent mixing as

\[
\frac{d\tilde{C}}{dz} = -\frac{J_{\text{benthic}}}{E_z}
\]  

(A6)

where \( J_{\text{benthic}} \) is an assumed known benthic flux and \( E_z \) is the turbulent eddy diffusivity.

The latter can be estimated by the semi-empirical equation (Businger and Arya, 1975)

\[
E_z = \kappa u_* h e^{-2h/H}
\]  

(A7)

where \( \kappa \) is von Karman’s constant (0.41) and \( u_* \) is the friction velocity. Finally, \( u_* \), the sediment surface roughness parameter, \( z_0 \), and the current velocity at the measuring height, \( \bar{u} \), are related by the classic log velocity profile

\[
\bar{u} = \frac{u_*}{\kappa} \ln \left( \frac{h}{z_0} \right)
\]  

(A8)
The model was applied to the eddy covariance data reported by Berg and Huettel (2008) for a shallow-water sandy sediments exposed to waves. Model parameter values in Table A1 were found to give good agreement between modeled and measured fluctuations in velocity and oxygen concentration.

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References


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Table A1. Wave model parameters used to produce results in Figs. 2 and 3.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water depth, $H$</td>
<td>140 cm</td>
</tr>
<tr>
<td>Measuring height, $h$</td>
<td>12 cm</td>
</tr>
<tr>
<td>Wave surface displacement amplitude, $a$</td>
<td>11 cm</td>
</tr>
<tr>
<td>Wave frequency, $f$</td>
<td>0.43 s$^{-1}$</td>
</tr>
<tr>
<td>Wavenumber, $k$</td>
<td>0.0089 rad cm$^{-1}$</td>
</tr>
<tr>
<td>Current velocity, $\bar{u}$</td>
<td>1 cm s$^{-1}$</td>
</tr>
<tr>
<td>Sediment surface roughness parameter, $z_0$</td>
<td>0.2 cm</td>
</tr>
<tr>
<td>Benthic oxygen flux (uptake), $J_{\text{benthic}}$</td>
<td>$-368$ mmol m$^{-2}$ d$^{-1}$</td>
</tr>
</tbody>
</table>
Figure 1. Example of traditional time lag correction of 8 Hz eddy covariance data measured with a dual oxygen-temperature sensor in unidirectional river flow. The “best” flux estimate is defined as the maximum numeric flux value and corresponds to an optimal time shift of 0.875 s.
Figure 2. Illustration, using modeled data, of the substantial error, or time lag bias, that can arise in eddy flux estimates from data measured in the presence of waves. Parameters for the model were taken from Berg and Huettel (2008). (a) Fluctuations due to wave motion only in vertical velocity ($\tilde{w}$), oxygen concentration ($\tilde{O}_2$), and vertical displacement, ($\tilde{z}$, see its definition and use in text). (b) Time lag bias (blue line) at different imposed time shifts, relative to the assumed real flux (red line) which was used to parameterize the model.
Figure 3. Reduction in maximum bias with increasing current velocity. The star represents the modeled data shown in Fig. 2b where the maximum bias is 180% of the assumed real flux. Except for the current velocity, and derived friction velocity and turbulent eddy diffusivity (see Appendix), all other model parameters were kept constant.
Figure 4. Illustration of the new time lag correction for a 15 min long data segment measured during nighttime over a dense seagrass meadow. (a) Fifteen s data segment of the larger 15 min segment showing oxygen concentration fluctuations due to wave motions before ($\tilde{O}_2$) and after the time lag correction ($\tilde{O}_{2\text{ corr}}$), and vertical displacement ($\tilde{z}$) calculated from Eq. (1). (b) Eddy flux calculated for the 15 min period by stepwise shifting oxygen data forward (up to 0.25 s) and backward (up to 1.25 s) in time and the associated cross-correlation of $\tilde{z}$ and $\tilde{O}_2$. (c) Oxygen flux calculated for the following time shifts: the traditional time shift correction (old corr.), illustrated in Fig. 1, no time shift (no corr.), and the new time lag correction (new corr.). The latter was defined as the shift that gave a minimum in cross-correlation of $\tilde{z}$ and $\tilde{O}_2$ as illustrated in (b).
Technical Note: Time lag correction of aquatic eddy covariance data

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Figure 5. Application of the new time lag correction applied to a 4 h long data segment measured over a dense seagrass meadow. (a) Sixty s segment of wave-driven variation in oxygen concentration after correction ($\tilde{O}_{2,corr}$) and vertical displacement ($\tilde{z}$) as calculated from Eq. (1). (b) Fifteen min averages of the two horizontal velocity components ($u$ and $v$), water depth, and significant wave height. (c) Oxygen flux, one per 15 min, determined without and with the new correction, light (PAR) measured above the seagrass canopy, and the time shift. (d) Average flux for nighttime (Time > 18.25 h) before and after correction.
Figure 6. Application of the new time lag correction applied to a 16 h long data segment measured over a permeable sandy sediment and reported earlier by Berg and Huettel (2008). (a) Sixty s segment of wave-driven variation in oxygen concentration after correction (\(O_2\) corr) and vertical displacement (\(\tilde{z}\)) as calculated from Eq. (1). The data are from when the wave action was at its maximum (Time \(\sim\) 620 min). (b) Fifteen min averages of the two horizontal velocity components (\(u\) and \(v\)), water depth, and significant wave height. (c) Oxygen flux, one per 15 min, determined without and with the new correction, light measured above the sand, and the time shift. (d) Average flux for nighttime (450 min < Time < 1095 min) before and after correction and measured concurrently with in situ chambers.