

# Early-phase Dose-finding Design for Molecularly Targeted Agents

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# Outline

- ▶ Background
- ▶ Models & inference
- ▶ Dose-finding algorithm
- ▶ Simulation results
- ▶ Conclusions

# Traditional Dose-finding

- ▶ Primary goal for a cytotoxic agent is to identify MTD
- ▶ Recommended dose further investigated in Phase II to evaluate efficacy
- ▶ Common assumption for cytotoxics is both efficacy and toxicity increase monotonically with dose
- ▶ Recent development of molecularly targeted agents (MTA's) challenges this assumption

# Dose-finding For Molecularly Targeted Agents

- ▶ Toxicity may be minimal
  - ▶ Often reasonable to assume monotonicity
- ▶ Dose-efficacy curves may be non-monotonic
- ▶ Goal is to find optimal biological dose (OBD)
  - ▶ Defined by dose with acceptable toxicity that maximizes efficacy

## Published Methods For MTA's

- ▶ Hunsberger, Rubinstein, Dancey, Korn; *Statist Med* 2005
- ▶ Mandrekar, Cui, Sargent; *Statist Med* 2007
- ▶ Polley, Cheung; *Biometrics* 2008
- ▶ Hoering, LeBlanc, Crowley; *Clin Cancer Res* 2011
- ▶ Hoering, Mitchell, LeBlanc, Crowley; *Clin Trials* 2013
- ▶ Yin, Zheng, Xu; *Statist Med* 2013

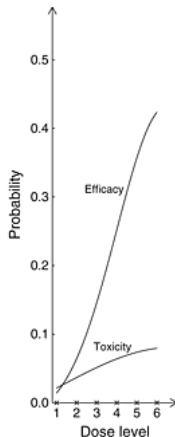
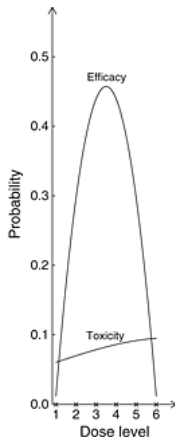
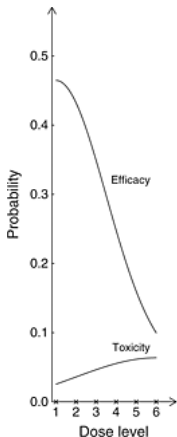
# Non-monotone Dose-efficacy Curves

- ▶ May exhibit unimodal or plateau relationships
  - ▶ Increase initially, then decrease or remain constant
- ▶ Suppose we have a set of  $I$  doses,  $\{d_1, \dots, d_I\}$  and probability of efficacy at  $d_i$  is denoted,  $\pi_E(d_i)$
- ▶ The goal is to find OBD,  $d_\nu \in \{d_1, \dots, d_I\}$ , defined by

$$\pi_E(d_1) \leq \dots \leq \pi_E(d_\nu) \geq \dots \geq \pi_E(d_I).$$

# Possible Dose-toxicity/efficacy Curves

Yin, Zheng, Xu; *Statist Med* 2013



## Example

- ▶ Phase I study of Baviximab in patients with advanced solid tumors (Gerber et al.; *Clinical Cancer Research*, 2011)
- ▶ Four available dose levels (0.1, 0.3, 1, 3 mg/kg)
- ▶ Goal of the study was dose escalation to the OBD, rather than MTD
- ▶ "... for monoclonal antibodies, the MTD may not correspond to optimal efficacy..."



# Overall Strategy

- ▶  $d_\nu$  corresponds to the peak of unimodal curve or beginning of plateau
- ▶ Peak could occur at any of the  $I$  available levels
  - ▶ Non-decreasing probabilities before the peak, non-increasing probabilities after peak
- ▶ Overall strategy is to formulate a set of possible dose-efficacy relationships corresponding to various “peak” locations

# Possible Dose-efficacy Curves

1. monotone decreasing: peak at  $d_1$   
 $\pi_E(d_4) \leq \pi_E(d_3) \leq \pi_E(d_2) \leq \pi_E(d_1)$
2. monotone increasing: peak at  $d_4$   
 $\pi_E(d_1) \leq \pi_E(d_2) \leq \pi_E(d_3) \leq \pi_E(d_4)$ .
3. unimodal or plateau: peak at  $d_2$   
 $\pi_E(d_1) \leq \pi_E(d_3) \leq \pi_E(d_4) \leq \pi_E(d_2)$
4. unimodal or plateau: peak at  $d_3$   
 $\pi_E(d_1) \leq \pi_E(d_2) \leq \pi_E(d_4) \leq \pi_E(d_3)$ .

# Modeling Toxicity - CRM

- ▶ The probability of DLT at dose level  $d_i$  is

$$\pi_T(d_i) \approx F(d_i, \beta) = p_i^{\exp(\beta)}$$

- ▶ After  $j$  inclusions, DLT probability estimates

$$\hat{\pi}_T(d_i) = F(d_i, \hat{\beta}_j)$$

define an acceptable set of doses based on a maximum acceptable toxicity rate  $\phi_T$

# Models For Efficacy

- ▶ Suppose there are  $K$  dose-efficacy model possibilities under investigation.
- ▶ For a particular model,  $k$ , the probability of efficacy modeled by

$$\pi_E(d_i) \approx G_k(d_i, \theta) = q_{ik}^{\exp(\theta)}$$

for a class of working dose-efficacy models,  $G_k(d_i, \theta)$

- ▶  $0 < q_{1k} < \dots < q_{Ik} < 1$  represents the skeleton of model  $k$ .

# Inference

- ▶ Prior probabilities on each model  $\tau(k) = \{\tau(1), \dots, \tau(K)\}$  and prior distribution,  $g(\theta)$ , on  $\theta$
- ▶ After inclusion of the first  $j$  patients into the study, the likelihood under model  $k$  is given by

$$L_k(\theta \mid \mathcal{D}_j) = \prod_{\ell=1}^j \{G_k(x_\ell, \theta)\}^{z_\ell} \{1 - G_k(x_\ell, \theta)\}^{(1-z_\ell)}$$

which, for each model, can be used in order to generate the posterior mean,  $\hat{\theta}_{jk}$ , of parameter  $\theta$ .

# Model Selection

- ▶ The posterior probabilities of the models given the data are

$$\omega(k | \mathcal{D}_j) = \frac{\tau(k) \int L_k(\theta | \mathcal{D}_j) g(\theta) d\theta}{\sum_{k=1}^K \tau(k) \int L_k(\theta | \mathcal{D}_j) g(\theta) d\theta}.$$

- ▶ When a new patient is to be enrolled, we choose a single model,  $k^*$ , with the largest posterior probability such that

$$k^* = \arg \max_k \omega(k | \mathcal{D}_j)$$

# Model Selection in CRM

- ▶ Bayesian model averaging CRM (Yin, Yuan; *JASA* 2009)
- ▶ Extended model-based designs for more complex dose-finding studies (O'Quigley, Conaway; *Statist Med* 2011)
- ▶ Posterior maximization and averaging for Bayesian working model choice in the CRM (Daimon, Zohar, O'Quigley; *Statist Med* 2011)
- ▶ CRM for partial ordering (Wages, Conaway, O'Quigley; *Biometrics* 2011)

# Efficacy Probability Estimates

- ▶ Take the working model,  $G_{k^*}(d_i, \theta)$ , associated with  $k^*$  to generate efficacy probability estimates at each dose.
- ▶ Compute the posterior probability of a response for  $d_i$

$$\hat{\pi}_E(d_i) = G_{k^*}(d_i, \hat{\theta}_{jk^*})$$

from which we can make decisions regarding allocation.



# Dose-finding Algorithm

- ▶ Overall, allocate the next entered patient to the dose estimated to be the most efficacious, among those with acceptable toxicity.
- ▶ Define the set of “acceptable” doses as

$$\mathcal{A}_j = \{d_i : \hat{\pi}_T(d_i) \leq \phi_T; i = 1, \dots, I\}.$$

- ▶ The allocation algorithm depends upon the amount of data that has been observed so far in the trial.

# Randomization Phase

- ▶ For doses in  $\mathcal{A}_j$ , calculate a randomization probability  $R_i$ ,

$$R_i = \frac{\hat{\pi}_E(d_i)}{\sum_{d_i \in \mathcal{A}_j} \hat{\pi}_E(d_i)}$$

and randomize the next patient or cohort of patients to dose  $d_i$  with probability  $R_i$ .

- ▶ Switch to a phase in which we simply allocate according to the maximum estimated efficacy probability among the acceptable doses.

# Maximization Phase

- ▶ Among the doses contained in  $\mathcal{A}_j$ , we allocate the  $(j + 1)$ th patient cohort to the dose  $x_{j+1}$  according to the estimated efficacy probabilities,  $\hat{\pi}_E(d_i)$ , such that

$$x_{j+1} = \arg \max_{d_i \in \mathcal{A}_j} \hat{\pi}_E(d_i)$$

- ▶ The optimal dose is the recommended dose  $d_i = x_{n+1}$  for the hypothetical  $(n + 1)$ th patient after the inclusion of the maximum sample size of  $n$  patients.

# Design Specifications

- ▶ Skeleton for toxicity,  $p_i = \{0.01, 0.08, 0.15, 0.22, 0.29, 0.36\}$
- ▶ Define maximum acceptable toxicity rate  $\phi_T = 0.33$
- ▶ Total sample size  $N = 48$
- ▶ Randomization phase sample size  $n_R = 12$
- ▶ Each of the  $k$  models has Normal prior distribution on  $\theta$

$$g(\theta) \sim \mathcal{N}(0, 1.34)$$

# Skeletons For Unimodal Relationships

- ▶ peak at  $d_6[k = 1]$   
{0.10, 0.20, 0.30, 0.40, 0.50, **0.60**}
- ▶ peak at  $d_5[k = 2]$   
{0.20, 0.30, 0.40, 0.50, **0.60**, 0.50}
- ▶ peak at  $d_4[k = 3]$   
{0.30, 0.40, 0.50, **0.60**, 0.50, 0.40}
- ▶ peak at  $d_3[k = 4]$   
{0.40, 0.50, **0.60**, 0.50, 0.40, 0.30}
- ▶ peak at  $d_2[k = 5]$   
{0.50, **0.60**, 0.50, 0.40, 0.30, 0.20}
- ▶ peak at  $d_1[k = 6]$   
{**0.60**, 0.50, 0.40, 0.30, 0.20, 0.10}

# Skeletons For Plateau Relationships

- ▶ plateau at  $d_1[k = 7]$   
 $\{0.60, 0.60, 0.60, 0.60, 0.60, 0.60\}$
- ▶ plateau at  $d_2[k = 8]$   
 $\{0.50, 0.60, 0.60, 0.60, 0.60, 0.60\}$
- ▶ plateau at  $d_3[k = 9]$   
 $\{0.40, 0.50, 0.60, 0.60, 0.60, 0.60\}$
- ▶ plateau at  $d_4[k = 10]$   
 $\{0.30, 0.40, 0.50, 0.60, 0.60, 0.60\}$
- ▶ plateau at  $d_5[k = 11]$   
 $\{0.20, 0.30, 0.40, 0.50, 0.60, 0.60\}$
- ▶ Assume, a priori, that each skeleton is equally likely and set  $\tau(k) = 1/11$

# Association Between Toxicity & Efficacy

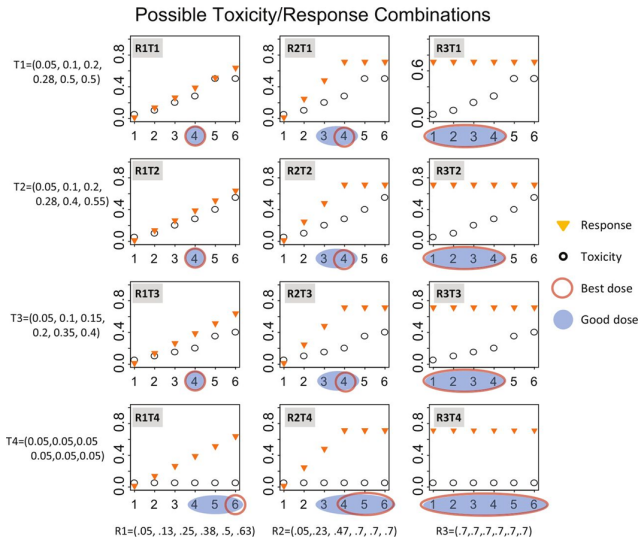
- ▶ Association between toxicity and efficacy is ignored in modeling
- ▶ Simulation studies assess the sensitivity of method to association between toxicity and efficacy
- ▶ Correlated binary responses generated under various values of association parameter  $\psi$
- ▶ Results presented with  $\psi = 4.6$  as in Hoering et al. (*Clinical Trials*, 2013)

## Dose-finding in Hoering et al. (2013)

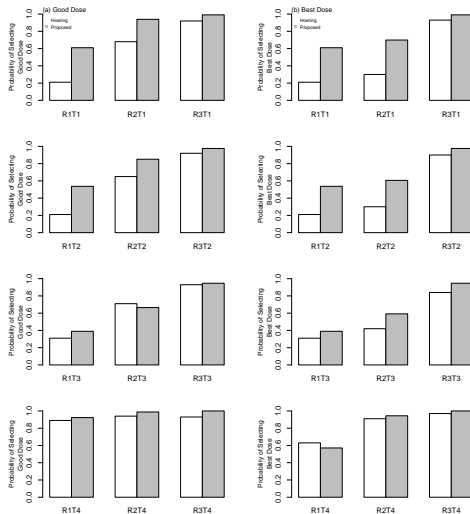
- ▶ 3+3 design in Phase I to find recommend dose (RD) for Phase II
- ▶ In Phase II, randomize 48 patients to one of three arms (dose levels)
  - ▶ RD-1, RD, RD+1
- ▶ Choose dose with highest efficacy that is also safe (DLT rate  $\leq$  33%).
- ▶ Authors define **best** dose as the level that maximizes efficacy while assuring safety; **good** dose as level where efficacy is above predefined boundary while maintaining safety.



## Hoering et al. Scenarios



## Simulation Results



# Unimodal Dose-efficacy Curves

- ▶ Scenario 1 ( $\pi_T, \pi_E$ )
  - ▶  $\{(0.05, 0.20), (0.10, 0.40), (0.25, 0.60), (0.45, 0.80), (0.60, 0.55)\}$
  - ▶ Peak of d-e curve occurs outside acceptable set
- ▶ Scenario 2 ( $\pi_T, \pi_E$ )
  - ▶  $\{(0.08, 0.20), (0.12, 0.40), (0.20, 0.60), (0.30, 0.80), (0.42, 0.55)\}$
  - ▶ Peak of d-e curve occurs at edge of acceptable set
- ▶ Scenario 3 ( $\pi_T, \pi_E$ )
  - ▶  $\{(0.06, 0.20), (0.08, 0.40), (0.14, 0.60), (0.20, 0.80), (0.30, 0.55)\}$
  - ▶ Peak of d-e curve occurs inside acceptable set

## Results

True DLT prob.	0.05	0.10	0.25	0.45	0.60
True Eff prob.	0.20	0.40	0.60	0.80	0.55
% selection	0.04	0.19	<b>0.53</b>	0.24	0.00
% allocation	0.12	0.26	<b>0.35</b>	0.23	0.03
True DLT prob.	0.08	0.12	0.20	0.30	0.42
True Eff prob.	0.20	0.40	0.60	0.80	0.55
% selection	0.04	0.17	0.29	<b>0.50</b>	0.01
% allocation	0.13	0.23	0.25	<b>0.34</b>	0.05
True DLT prob.	0.06	0.08	0.14	0.20	0.30
True Eff prob.	0.20	0.40	0.60	0.80	0.55
% selection	0.04	0.13	0.19	<b>0.62</b>	0.03
% allocation	0.10	0.19	0.20	<b>0.43</b>	0.07

$N = 30; n_R = 10; \phi_T = 0.35, \psi = -2$

# Conclusions

- ▶ Bivariate extension of CRM for effectively estimating optimal dose in early-phase trials of targeted agents.
- ▶ Good operating characteristics when compared to published method in area.
- ▶ Extension includes relaxing monotonicity assumption for toxicity
  - ▶ For trials of dual-agent combinations
  - ▶ Use partial order CRM (Wages, Conaway, O'Quigley; *Biometrics* 2011) to estimate DLT probabilities
- ▶ Exploring stopping rules for toxicity and efficacy
- ▶ Modifications for delayed response outcomes

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