Quantum Interference of Ultrastable Twin Optical Beams

Sheng Feng and Olivier Pfister*

Department of Physics, University of Virginia, 382 McCormick Road, Charlottesville, Virginia 22904-4714, USA
(Received 30 September 2003; published 21 May 2004)

We report the first measurement of the quantum phase-difference noise of an ultrastable nondegenerate optical parametric oscillator that emits twin beams classically phase locked at exact frequency degeneracy. The measurement illustrates the property of a lossless balanced beam splitter to convert number-difference squeezing into phase-difference squeezing, and thus provides indirect evidence for Heisenberg-limited interferometry using twin beams. This experiment is a generalization of the Hong-Ou-Mandel interference effect for continuous variables and constitutes a milestone towards continuous-variable entanglement of bright, ultrastable nondegenerate beams.

DOI: 10.1103/PhysRevLett.92.203601

PACS numbers: 42.50.Dv, 03.67.Mn, 42.50.St, 42.65.Yj

Nonclassical interference of highly excited boson modes is of fundamental interest for ultraprecise physical measurements, such as Heisenberg-limited interferometry [1] and spectroscopy [2], which find applications in ultimate-sensitivity measurements such as gravitational-wave detection [3] and modern atomic clocks [4]. Moreover, the quantum noise reduction (squeezing) at the heart of Heisenberg-limited measurements is connected to continuous-variable entanglement [5], of interest for quantum information and communication [6]. Preliminary Heisenberg-limited interferometers with \( N = 2 \) bosons have been realized with twin photons [7] and trapped ions [2]. Ultrasensitive interferometry, however, requires \( N \gg 1 \), and continuous-variable quantum optics and squeezed states are the tools of choice here. The use of Bose-Einstein condensates has been proposed [8] and progress has been made in this direction [9]. Recently, Silberhorn et al. made a beautiful demonstration of continuous-variable entanglement of picosecond-pulsed optical beams, by simultaneous squeezing of the number sum and of the phase difference [10]. For high-precision measurements, however, stable cw beams are preferable. One interesting system for this purpose is the ultrastable nondegenerate optical parametric oscillator (OPO), which emits intense twin beams. In a type II OPO, these twin beams are orthogonally polarized. It is thus easy to separate them spatially and to subsequently make their polarizations parallel. Then, the twin beams can be made indistinguishable by locking their frequency difference to zero, which has been an experimental challenge. This Letter reports the first experimental demonstration of nonclassical interference of such macroscopic boson fields.

In general, a quantum interference experiment consists of “splitting” a quantum field into two subfields, each experiencing its own phase evolution, and then “recombining” these subfields and performing a measurement. The corresponding probability distribution presents fringes which give information about the phase difference of the two subfields. Examples include the Mach-Zehnder interferometer for light and the Ramsey interferometer for matter, which are isomorphic to each other. “Nonclassical interference” may either mean that waves of a nonclassical nature are involved (e.g., matter waves) or that their behavior itself has no classical optical equivalent. The latter situation is what interests us, and is determined by the role of the vacuum modes of the quantum field, i.e., the physics of the “splitting.” The physics of the beam splitter (Fig. 1) takes center stage here and also determines the phase measurement noise. Take the example of an initial \( N \)-photon Fock state \( \ket{k_a, \bar{\epsilon}, \omega; N_a} \), where \( k \) and \( \bar{\epsilon} \) are the unit wave and polarization vectors and \( \omega \) is the angular frequency. The beam-splitter output is given by the interference of this state with the corresponding polarization- and frequency-degenerate vacuum state \( \ket{k_b, \bar{\epsilon}, \omega; 0_b} \). As was first demonstrated by Caves in 1980 [11], this yields a (classically intuitive) binomial probability distribution of the photon number between modes \( c \) and \( d \), with standard deviation \( \Delta N_{\text{out}} = \Delta (N_c - N_d) \approx N^{1/2} \). Using the Heisenberg inequality between number and phase differences \( \Delta N \Delta \phi \geq 1 \), we obtain \( \Delta \phi_{\text{out}} \approx N^{-1/2} \), which we call the classical limit of an interferometer. Note that this limit becomes \( \langle N \rangle^{-1/2} \) for any input state of average photon number \( \langle N \rangle \) and is independent of the photon statistics of the input [11]. The classical limit is the limit of all interferometers whose input splitting involves unmodified vacuum modes, including last-generation atomic clocks [4]. It is not, however, the ultimate phase

\[
a = \frac{1}{\sqrt{2}} (a + ib)
\]

\[
b = \frac{1}{\sqrt{2}} (ia + b)
\]

\[
c = \frac{1}{\sqrt{2}} (a + ib)
\]

\[
d = \frac{1}{\sqrt{2}} (ia + b)
\]

FIG. 1. Beam splitter. The input and output modes have annihilation operators \( (a, b) \) and \( (c, d) \), respectively. The reflection/transmission coefficients are \( r = it = 2^{-1/2} \). The beams are aligned so that \( \hat{k}_{c,d} = \hat{k}_{b,a} \).
have been made. One of the simplest ones, from Holland et al. [13], which was realized experimentally by Xiao et al. [14]. A number of other proposals have been made. One of the simplest ones, from Holland and Burnett [15], is to use number-correlated, degenerate input states of the general (ideal) density matrix:

$$\sum_{n,p} \rho_{n,p} |\hat{k}_a, \hat{\epsilon}, \omega; n\rangle \langle \hat{k}_b, \hat{\epsilon}, \omega; n|$$

which we will call twin modes. Such states give the Heisenberg limit as well [16], even though the measurement procedure is complicated by the fact that the output intensities show no interference fringes. A Bayesian detection procedure [15] was proposed to remedy the situation, and we have confirmed its experimental feasibility by numerically simulating nonideal conditions [17].

A crucial requirement for the performance of twin-mode interferometry is the exact polarization and frequency degeneracy, i.e., indistinguishability, of the input states. This is the key to the nonclassical interference that maximizes $\Delta N_{\text{out}}$ and therefore minimizes $\Delta \phi_{\text{out}}$. A good illustration of this point is the simplest possible case of a twin photon pair $|\hat{k}_a, \hat{\epsilon}, \omega; 1\rangle, |\hat{k}_b, \hat{\epsilon}, \omega; 1\rangle$, i.e., the Hong-Ou-Mandel (HOM) interferometer [18], recently revisited by Santori et al. using two consecutive photons from the same source [19]. Out of the four possible beam-splitter scattering probability amplitudes, the two corresponding to the output state $|\hat{k}_c, \hat{\epsilon}, \omega; 1\rangle, |\hat{k}_d, \hat{\epsilon}, \omega; 1\rangle$ interfere destructively because of indistinguishability of the input photons, i.e., the degeneracy of the input modes. This maximizes $\Delta N_{\text{out}}$, giving $\Delta N_{\text{out}} = 2$ instead of $\sqrt{2}$. This effect disappears if the beam splitter is misaligned ($\hat{k}_{c,d} \neq \hat{k}_{b,a}$), or if $\hat{\epsilon}_a \neq \hat{\epsilon}_b$ or $\omega_a \neq \omega_b$. If any of the previous conditions is true, for example $\omega_a \neq \omega_b$, then there are four input modes instead of two: The beam-splitter input state becomes $|\hat{k}_a, \hat{\epsilon}, \omega; 1\rangle_a |\hat{k}_b, \hat{\epsilon}, \omega_b; 0\rangle_0 \otimes |\hat{k}_b, \hat{\epsilon}, \omega_b; 0\rangle_0 |\hat{k}_a, \hat{\epsilon}, \omega_a; 1\rangle_b$, and the photons interfere only with their respective vacuum modes instead of interfering with each other. One then obtains the probabilistic mixture of two single-photon cases: No destructive interference occurs and all possible output states are equiprobable.

Of even greater interest is the situation where the beam-splitter input is $|\hat{k}_a, \hat{\epsilon}, \omega; N\rangle_a |\hat{k}_b, \hat{\epsilon}, \omega; N\rangle_b$ [20] or, better yet, the more general form expressed by Eq. (1), for which the physics is identical [16]. Close approximations to such states are generated above threshold in a type II OPO, which emits intense, laserlike, cross-polarized, number-difference squeezed beams [21] that can be frequency stabilized by the use of standard techniques of laser metrology [22,23] or optical self-locking [24]. However, squeezing and ultrastable frequency degeneracy have never been combined in the same experiment before, which is the sine qua non condition for the observation of the nonclassical twin-beam interference. We now present the experimental observation of this effect.

The principal difficulty of the experiment resides in creating exactly frequency-degenerate twin beams. A type II OPO has a clustered emission spectrum (see [25] and references therein) and the mode-hop length in our case is $\lambda/500$, compared to $\lambda/2$ for a laser. High performance servo loops are therefore essential to keep the OPO emission at the degenerate mode $\omega_a = \omega_b$, where $\omega_{a,b}$ are the twin-beam frequencies. Our experimental setup is sketched in Fig. 2 and is described in more detail in Refs. [25,26].

The OPO consists of a temperature-stabilized Na:KTiOPO4 nonlinear crystal, in which pump photons at 532 nm are downconverted to cross-polarized pairs at 1064 nm, and an optical cavity formed by mirrors $M_l, M_o$. The 1064 nm twin beams exit through $M_o$ to the right of the figure. The reflected pump beam is used for locking the cavity and a weak leak at 1064 nm through $M_l$ is used for locking the phase difference of the twin beams. With only the temperature and cavity locks, the frequency difference error is $\pm 150$ kHz [25]. Adding the optical phase-lock loop (PLL) reduces this error by more than 5 orders of magnitude to less than 1 Hz (Fig. 3), while keeping the frequency difference continuously tempera-
function of the cold-cavity FWHM, $T$ is the free spectral range, and $\xi$ is the correlation coefficient, $T$ is the output coupler transmissivity, and $\lambda$ is the single-pass intensity loss. Equations (4) and (5) can also be understood qualitatively: For very short observation times compared to the cavity storage time ($u \gg 1$), the photon correlations are destroyed by the random cavity-exit times of each twin of a pair and no squeezing is present [4]. However, if one integrates the photon counting over at least the cavity storage time ($u \leq 1$), then correlations become visible again and squeezing of $N_-$ is observed within the cavity linewidth. Hence, the conjugate variable $\phi$ should be antisqueezed within the cavity linewidth, where the OPO’s double resonance condition is relaxed, since the phase difference is fixed to a multiple of $2\pi$ by double resonance only for times not exceeding the cavity storage time ($u \geq 1$). For longer times ($u \ll 1$), the phase difference noise becomes dominated by the Schawlow-Townes drift of the OPO phase difference [30]. Record amounts of number-difference squeezing ($-8.5$ dB) have been obtained by the group of Fabre and Giacobino [21], but the demonstration of phase-difference antisqueezing (5), which necessitates twin-beam indistinguishability, has not been previously achieved.

Figures 4(a) and 4(b) display the intensity-difference spectra for distinguishable and undistinguishable OPO beams, respectively. In Fig. 4(a), the OPO frequencies $\omega_{a,b}$ are separated by at least the free spectral range, i.e., are totally distinguishable. The phase-difference noise spectrum (blue line) is a measure of the total shot noise, each beam interfering with vacuum in the other input.
port. No HOM-type quantum interference takes place. In Fig. 4(b), the OPO frequencies are phase locked within less than 1 Hz of each other. In this case, the twin beams are totally indistinguishable and the phase-difference spectrum (red line) becomes extremely noisy for \( \nu \leq \delta \). This noise is well fitted by Eq. (5) despite additional technical noise (mainly pump intensity noise) at frequencies below 2 MHz. The fit parameters are entirely determined by the fit of the intensity difference spectrum (green line). This good agreement indicates that the OPO output is in a minimum uncertainty state. The intensity-difference noise is not affected by indistinguishability, even though we obtain different squeezing levels: \(-5.5 \text{ dB} \) (\(-6 \text{ dB} \) when accounting for detection noise) in Fig. 4(a) but only \(-3 \text{ dB} \) in Fig. 4(b). We believe that this is due, in the latter case, to partial overlap of the beams with grey tracks (optical damage) in the crystal, which induces differential losses that cannot be balanced out. This is consistent with the slight increases of \( \delta \) and of residual classical noise in Fig. 4(b), compared to Fig. 4(a).

In conclusion, we have observed, for the first time, the HOM interference of macroscopic boson modes. Although their quantum state is much more complicated than, say, a twin Fock state, nonclassical interference does take place nonetheless, as was predicted in \([5,16,28]\). The independence of the quantum interference from common-mode photon statistics stems from beam-splitter physics, not from the light source itself. This is identical to the independence of the classical limit from the beam splitter, we expect a minimum uncertainty state antisqueezed in \( N_- \) and squeezed in \( \phi_- \), from the beam-splitter’s property of swapping number- and phase-difference fluctuations \([15,31]\). Finally, the level of performance of this experiment is precisely that which is required in order to test the proposal of Reid and Drummond to create bright ultra-stable EPR beams \([5]\). Because the OPO frequency difference is tunable in our experiment, we expect to be able to entangle frequency nondegenerate fields.

We thank Ken Nelson and Harvey Sugerman for their help with electronics design and construction, and Dan Perlov from Coherent-Crystal Associates for help with understanding Na:KTP. This work is supported by ARO Grants No. DAAD19-01-1-0721 and No. DAAD19-02-1-0104, and in part by NSF Grants No. PHY-0240532 and No. EIA-0323623.

*Author to whom correspondence should be addressed.
Electronic address: opfister@virginia.edu